



Unified International
Mathematics Olympiad

UNIFIED INTERNATIONAL MATHEMATICS OLYMPIAD (UPDATED)

CLASS - 9

Question Paper Code : 4P104

KEY

1	2	3	4	5	6	7	8	9	10
A	B	D	C	A	D	A	A	C	A
11	12	13	14	15	16	17	18	19	20
C	B	C	D	B	B	B	B	A	A
21	22	23	24	25	26	27	28	29	30
D	C	A	C	C	D	B	B	D	C
31	32	33	34	35	36	37	38	39	40
A,C,D	A,B,C	A,B	A,B,C	A,C,D	C	D	C	D	A
41	42	43	44	45	46	47	48	49	50
C	C	C	B	D	B	C	D	B	A

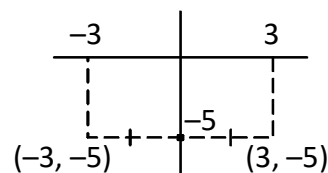
SOLUTIONS

MATHEMATICS - 1 (MCQ)

01. (A) $\sqrt{4a^2 + ab^2 + 16c^2 + 12a - 24bc - 16ca} =$
 $\sqrt{(2a)^2 + (3b)^2 + (-4c)^2 + 2(2a)(3b) +$
 $2(3b)(-4c) + 2(-4c)(2a)}$
 $= \sqrt{(2a + 3b - 4c)^2}$

02. (B) $x^2 + 2x + 1 - x^2 + 1 = 2x^2 + x - 2(x^2 + 3x +$
 $2) + 20$
 $2x + 2 = 2x^2 + x - 2x^2 - 6x - 4 + 20$
 $7x = 16 - 2 \Rightarrow x = 2$

03. (D)



04. (C)

$\triangle ADH \cong \triangle JIH$ [\because ASA congruency]

\therefore Area of $\triangle ADH$ = area of $\triangle JIH$

\therefore Shaded area : Total area = $1 : 3 = \frac{1}{3}$

05. (A) Given $\frac{4}{3}\pi r^3 = \frac{1}{3}\pi \times 6 \times 6 \times 24 \text{ cm}^3$

$r = 6 \text{ cm}$

06. (D) $a^2 + 6ab + 9b^2 + b^2 + 2bc + c^2 + 4c^2 - 16c + 42 = 0$

$(a + 3b)^2 + (b + c)^2 + (2c - 4)^2 = 0$

Sum of three perfect squares is zero then each term must be zero

$\therefore a = -3b, b = -c, 2c = 4$

$a = 6, b = -2, c = 2$

$\therefore a - b + c = 6 + 2 + 2 = 10$

07. (A) $9^{\frac{1}{3}}, 11^{\frac{1}{4}}, 17^{\frac{1}{6}}$

$9^{\frac{4}{12}}, 11^{\frac{3}{12}}, 17^{\frac{2}{12}}$

$\sqrt[12]{9^4}, \sqrt[12]{11^3}, \sqrt[12]{17^2}$

$x = \sqrt[12]{6561} \quad y = \sqrt[12]{1331} \quad z = \sqrt[12]{289}$

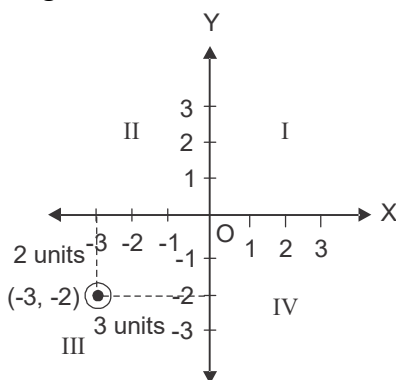
$\therefore x > y > z.$

08. (A) The perpendicular distance of a point from x -axis = 2 units.

The perpendicular distance of a point from y -axis = 3 units

Given, that the point lies in the III Quadrant

\Rightarrow Both the coordinates of the point are negative.



\therefore The required coordinates of the point are $(-3, -2).$

09. (C)

$S = \frac{a+b+c}{2} = \frac{21m+20m+13m}{2} = \frac{54m}{2} = 27m$

$\Delta = \sqrt{S(s-a)(s-b)(s-c)}$

$= \sqrt{27 \times 6 \times 7 \times 14} \text{ m}^2$

$= \sqrt{3 \times 9 \times 2 \times 3 \times 7 \times 2 \times 7} \text{ m}^2$

$= 3 \times 3 \times 2 \times 7 \text{ m}^2$

$= 126 \text{ m}^2$

10. (A) Given $2r = 14 \text{ cm}$

$r = \frac{14 \text{ cm}}{2} = 7 \text{ cm}$

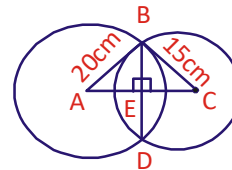
\therefore Height = $2r = 14 \text{ cm}$

Volume = $\pi r^2 h = \frac{22}{7} \times 7 \times 7 \times 14 \text{ cm}^3$

$= 2156 \text{ cm}^3$

$= \frac{2156}{1000} \text{ Litres} = 2.156 \text{ Litres}$

11. (C) Given $AB = 20 \text{ cm}$ & $BC = 15 \text{ cm}$



$AC = 25 \text{ cm}$ and $BD \perp AC$

In $\triangle ABE$, Let $AE = x \text{ cm} \Rightarrow EC = (25 - x) \text{ cm}$

$BE^2 = AB^2 - AE^2 = (20)^2 - x^2 = 400 - x^2$

$\rightarrow (1)$

In $\triangle BCE$, $BE^2 = BC^2 - EC^2 = (15)^2 - (25 - x)^2$

$= 225 - (625 - 50x + x^2)$

$= 225 - 625 + 50x - x^2$

$= 50x - x^2 - 400 \rightarrow (2)$

But eq (1) = eq (2)

$400 - x^2 = 50x - x^2 - 400$

$400 + 400 = 50x$

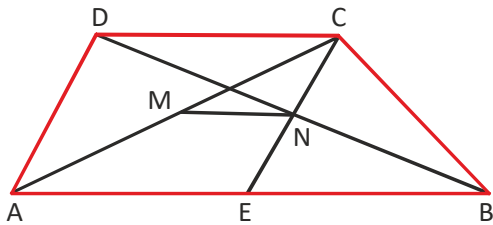
$x = \frac{800}{50} = 16$

$\therefore BE^2 = 400 - x^2 = 400 - 16^2 = 400 - 256 = 144$

$\therefore BE = \sqrt{144} \text{ cm} = 12 \text{ cm}$

$\therefore BD = 2BE = 2 \times 12 \text{ cm} = 24 \text{ cm}$

12. (B)



Const: Join CN and extend upto E

Proof: $\triangle CND \cong \triangle ENB$

[\because ASA Congruency]

\therefore CN = NE \Rightarrow 'N' is the mid point of CE & CD = BE

$$\text{In } \triangle ACE, MN = \frac{1}{2} AE = \frac{1}{2} (AB - BE)$$

$$= \frac{1}{2} (AB - CD) = 3 \text{ cm}$$

13. (C) $\frac{1}{x} = \frac{1}{9+4\sqrt{5}} \times \frac{9-4\sqrt{5}}{9-4\sqrt{5}} = \frac{9-4\sqrt{5}}{9^2 - (4\sqrt{5})^2}$

$$= 9 - 4\sqrt{5}$$

$$x + \frac{1}{x} = 9 + 4\sqrt{5} + 9 - 4\sqrt{5} = 18$$

Squaring on both sides

$$\left(x + \frac{1}{x}\right)^2 = 18^2$$

$$x^2 + 2 \times \cancel{x} \times \frac{1}{\cancel{x}} + \frac{1}{x^2} = 324$$

$$x^2 + \frac{1}{x^2} = 324 - 2 = 322$$

14. (D) Given $(x - 1)^8 = a^8 x^8 + a^7 x^7 + a^6 x^6 + \dots + a^1 x + a^0$

Given $(x - 1)$ is a factor of $f(x) = (x - 1)^8$

$$\therefore f(1) = 0$$

$$\therefore f(1) = a^8(1)^8 + a^7(1)^7 + a^6(1)^6 + \dots + a^1(1)^1 + a^0 = 0$$

$$\therefore a^8 + a^7 + a^6 + a^5 + a^4 + a^3 + a^2 + a^1 + a^0 = 0$$

15. (B) From options If $x = 3$ then

$$\sqrt{3+1} + \sqrt{6+3} = 2 + 3 = 5 \text{ (or)}$$

$$\text{Given } \sqrt{x+1} + \sqrt{2x+3} = 5$$

Squaring on both sides

$$(\sqrt{x+1} + \sqrt{2x+3})^2 = 5^2$$

$$x+1 + 2\sqrt{x+1}\sqrt{2x+3} + 2x+3 = 25$$

$$2(\sqrt{x+1})(\sqrt{2x+3}) = 25 - 4 - 3x$$

$$2(\sqrt{x+1}\sqrt{2x+3}) = 21 - 3x$$

Squaring on both sides

$$4(x+1)(2x+3) = (21-3x)^2 = 441 - 126x + 9x^2$$

$$4(2x^2 + 5x + 3) = 441 - 126x + 9x^2$$

$$8x^2 + 20x + 12 - 9x^2 + 126x - 441 = 0$$

$$-x^2 + 146x - 429 = 0$$

$$x^2 - 146x + 429 = 0$$

$$x^2 - 143x - 3x + 429 = 0$$

$$x(x - 143) - 3(x - 143) = 0$$

$$\therefore (x - 3)(x - 143) = 0$$

$x = 3$ (or) $x = 143$ but $x = 143$ does n't satisfy the given question

$$\therefore x = 3$$

16. (B) Let the height be 'x'

$$\therefore \text{Radius} = 1\frac{2}{3}x = \frac{5}{3}x$$

Given $2\pi rh = 4620 \text{ cm}^2$

$$\Rightarrow 2 \times \frac{22}{7} \times \frac{5x}{3} \times x = 4620 \text{ cm}^2$$

$$x^2 = \frac{4620 \times 7 \times 3}{2 \times 22 \times 5} \text{ cm}^2 = 21^2 \text{ cm}^2$$

$$x^2 = (21 \text{ cm})^2$$

$$\therefore x = 21 \text{ cm}$$

$$\therefore \text{Radius} = \frac{5}{3}x = \frac{5 \times 21}{3} \text{ cm} = 35 \text{ cm}$$

Total surface area = $2\pi r(h + r)$

$$= 2 \times \frac{22}{7} \times 35 \text{ cm} (21 + 35) \text{ cm}$$

$$= 220 \text{ cm} \times 56 \text{ cm} = 12320 \text{ cm}^2$$

$$\begin{aligned}
 17. (B) \quad & (a + b + c)^2 - (a - b - c)^2 = (a^2 + b^2 + c^2 + 2ab + 2bc + 2ca) - (a^2 + b^2 + c^2 - 2ab + 2bc - 2ca) \\
 & = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca - a^2 - b^2 - c^2 + 2ab - 2bc + 2ca \\
 & = 4ab + 4ca \\
 & = 4a(b + c)
 \end{aligned}$$

$$\begin{aligned}
 18. (B) \quad \text{LHS} \quad & \sqrt{\sqrt{3} - \sqrt{4 - \sqrt{5} - \sqrt{12 + 5 - 2\sqrt{12} \times \sqrt{5}}}} \\
 & \sqrt{\sqrt{3} - \sqrt{4 - \sqrt{5} - \sqrt{(\sqrt{12} - \sqrt{5})^2}}} \\
 & = \sqrt{\sqrt{3} - \sqrt{4 - \sqrt{5} - (\sqrt{12} - \sqrt{5})}} \\
 & = \sqrt{\sqrt{3} - \sqrt{4 - \sqrt{5} - \sqrt{12} + \sqrt{5}}} \\
 & = \sqrt{\sqrt{3} - \sqrt{4 - \sqrt{12}}} \\
 & = \sqrt{\sqrt{3} - \sqrt{(\sqrt{3})^2 + 1^2 - 2\sqrt{3}}} \\
 & = \sqrt{\sqrt{3} - \sqrt{(\sqrt{3} - 1)^2}} \\
 & = \sqrt{\sqrt{3} - \sqrt{3} + 1} \\
 & = \sqrt{1} = 1
 \end{aligned}$$

19. (A) Given $x^2 + x + 1 = 0$

$$\frac{x^2}{x} + \frac{x}{x} + \frac{1}{x} = 0$$

$$x + 1 + \frac{1}{x} = 0$$

$$x + \frac{1}{x} = -1$$

cubing on both sides

$$x^3 + \frac{1}{x^3} + 3x \times \frac{1}{x} \left(x + \frac{1}{x}\right) = -1$$

$$x^3 + \frac{1}{x^3} + 3(-1) = -1$$

$$x^3 + \frac{1}{x^3} = -1 + 3$$

$$x^3 + \frac{1}{x^3} = 2$$

cubing in both sides

$$\left(x^3 + \frac{1}{x^3}\right)^3 = 8$$

(OR) Given $x^2 + x + 1 = 0$

$$(x - 1)(x^2 + x + 1) = 0 \quad (x - 1)$$

$$x^3 - 1^3 = 0 \Rightarrow x^3 = 1$$

$$\therefore \left(x^3 + \frac{1}{x^3}\right)^3 = \left(1 + \frac{1}{1}\right)^3$$

$$= 2^3 = 8$$

20. (A) Given $\angle A + \angle C = 140^\circ$

and $\angle A : \angle C = 1 : 3$

$$\Rightarrow \angle A = 140^\circ \times \frac{1}{4} = 35^\circ$$

$$\text{and } \angle C = 140^\circ \times \frac{3}{4} = 35^\circ \times 3 = 105^\circ$$

In the quadrilateral

$$\angle A + \angle B + \angle C + \angle D = 360^\circ$$

$$\Rightarrow \angle B + \angle D = 360^\circ - (\angle A + \angle C)$$

$$= 360^\circ - 140^\circ$$

$$\therefore \angle B + \angle D = 220^\circ$$

Given that $\angle B : \angle D = 5 : 6$,

$$\angle B = 220^\circ \times \frac{5}{11} = 20^\circ \times 5 = 100^\circ$$

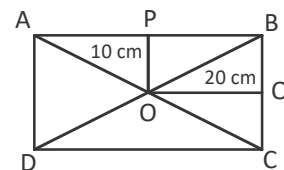
$$\text{and } \angle D = 220^\circ \times \frac{6}{11} = 20^\circ \times 6 = 120^\circ$$

$$\therefore \text{The required angles are } \angle A = 35^\circ, \angle B = 100^\circ, \angle C = 105^\circ \text{ and } \angle D = 120^\circ.$$

21. (D) $BC = AD = 2PO = 20$ cm

$$AB = DC = 2 \times OQ = 40$$
 cm

$$\text{Perimeter of rectangle} = 2(AB + BC) = 120$$
 cm



22. (C) Given $\left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2 = \left(\frac{34}{4} \text{ cm}\right)^2$

$$\frac{d_1^2}{4} + \frac{d_2^2}{4} = \frac{289}{4} \text{ cm}^2$$

$$\therefore d_1^2 + d_2^2 = 289$$

Given $d^1 + d^2 = 23 \text{ cm}$

squaring on both sides

$$d_1^2 + d_2^2 + 2d_1 d_2 = 529$$

$$289 + 2d^1 d^2 = 529$$

$$2d^1 d^2 = 240$$

$$\frac{2d_1 d_2}{4} = \frac{240}{4} \text{ cm}^2$$

$$\text{Area of rhombus} = \frac{d_1 d_2}{2} = 60 \text{ cm}^2$$

23. (A) Volumes ratio of sphere, cone & cylinder

$$= \frac{4}{3} \pi r^3 : \frac{1}{3} \pi r^2 h : \pi r^2 h$$

$$= \frac{4}{3} : \frac{2}{3} : 2$$

$$= \frac{2}{3} : \frac{1}{3} : 1$$

$$= 2 : 1 : 3$$

24. (C) Let the original radius be $r \text{ cm}$

$$\therefore \text{Original surface area} = 4\pi r^2$$

$$\text{New radius (R)} = r + 100\% r = r + r = 2r$$

$$\text{New are surface} = 4\pi R^2 = 4\pi(2r)^2$$

$$= 4(4\pi R^2)$$

$$\text{Increased area} = 4(4\pi R^2) - 4\pi r^2$$

$$= 3(4\pi r^2)$$

Increased area percentage

$$= \frac{3(4\pi r^2)}{4\pi r^2} \times 100 = 300\%$$

25. (C) Given $x + \frac{9}{x} = 6 \Rightarrow \frac{x^2 + 9}{x} = 6$

$$\Rightarrow x^2 - 6x + 9 = 0$$

$$\Rightarrow x^2 - 3x - 3x + 9 = 0$$

$$\Rightarrow x = 3$$

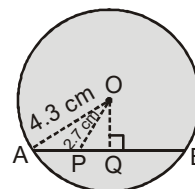
$$\therefore x^2 + \frac{9}{x^2} = 9 + \frac{9}{9} = 9 + 1 = 10$$

26. (D) $\triangle AOX \cong \triangle COY$ [\therefore ASA congruency]

$$\therefore OX = OY \quad [\therefore \text{CPCT}]$$

$$\therefore OX - OY = 0$$

27. (B) As shown in the figure, $OP = 2.7 \text{ cm}$ and $OA = 4.3 \text{ cm}$. Draw a perpendicular OQ to the chord AB . Clearly, $AQ = QB$. Since P divides AB in the ratio $7 : 10$, let AP be $7x$ and PB be $10x$.



$$\text{Also, } PQ = AQ - AP = \frac{AB}{2} - AP$$

$$= \frac{17x}{2} - 7x = 1.5x$$

By Pythagoras' theorem, we have, $AQ^2 + OQ^2 = AO^2$.

$$\text{Also, } OP^2 = PQ^2 + OQ^2.$$

$$\Rightarrow AQ^2 - PQ^2 = AO^2 - OP^2$$

$$\Rightarrow (8.5x)^2 - (1.5x)^2 = (4.3)^2 - (2.7)^2$$

$$\Rightarrow (10x)(7x) = 7(1.6)$$

$$\Rightarrow x^2 = 0.16 \text{ or } x = 0.4 \text{ cm.}$$

$$\therefore AB = 17x = 17 \times 0.4 = 6.8 \text{ cm}$$

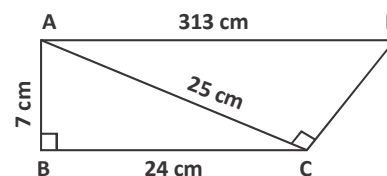
28. (B) $\angle RQP = 30^\circ + 225^\circ = 55^\circ$

$$\angle RQP = + x = 180^\circ$$

$$55^\circ + x = 180^\circ$$

$$x = 180^\circ - 55^\circ = 125^\circ$$

29. (D)



In $\triangle ABC$, $\angle B = 90^\circ$

$$AC^2 = AB^2 + BC^2$$

$$AB = 7 \text{ cm}$$

In $\triangle ACD$, $\angle ACD = 90^\circ$

$$AD^2 = AC^2 + CD^2$$

$$313^2 - 25^2 = CD^2$$

$$97,969 - 625 = CD^2$$

$$CD = \sqrt{97344}$$

$$CD = 312 \text{ cm}$$

Area of quad ABCD = Area of ABC + Area of ACD

$$\begin{aligned} &= \frac{1}{2} \times AB \times BC + \frac{1}{2} \times AC \times CD \\ &= \frac{1}{2} \times 7 \text{ cm} \times 24 \text{ cm} + \frac{1}{2} \times 25 \text{ cm} \times 312 \text{ cm} \\ &= 84 \text{ cm}^2 + 3900 \text{ cm}^2 \\ &= 3984 \text{ cm}^2 \end{aligned}$$

30. (C) ARPQ is a parallelogram

$$\therefore AR = PQ \text{ \& } PR = AQ$$

$$\therefore AR = PQ = \frac{AB}{2} = \frac{30 \text{ cm}}{2};$$

$$PR = AQ = \frac{AC}{2} = \frac{21 \text{ cm}}{2}$$

$$\begin{aligned} \therefore AR + RP + PQ + QA \\ &= \frac{30 \text{ cm}}{2} + \frac{30 \text{ cm}}{2} + \frac{21 \text{ cm}}{2} + \frac{21 \text{ cm}}{2} \\ &= 51 \text{ cm} \end{aligned}$$

MATHEMATICS - 2 (MAQ)

31. (A,C,D) Given $x = \frac{1}{2 - \sqrt{3}} \times \frac{2 + \sqrt{3}}{2 + \sqrt{3}} = 2 + \sqrt{3}$

$$x - 2 = \sqrt{3}$$

Squaring on both sides

$$x^2 - 4x + 4 = 3$$

$$x^2 - 4x + 1 = 0$$

$$x^2 - 4x + 1 \mid x^4 - x^3 + 6x^2 - 17x + 16(x^2 + 3x + 5)$$

$$x^4 - 4x^3 + x^2$$

$$(-) (+) (-)$$

$$\hline 3x^3 - 7x^2 - 17x + 16$$

$$3x^3 - 12x^2 + 3x$$

$$(-) (+) (-)$$

$$\hline 5x^2 - 20x + 16$$

$$5x^2 - 20x + 5$$

$$(-) (+) (-)$$

$$\hline (11)$$

$$x^2 - 4x + 1 \mid x^3 - 2x^2 - 7x + 2(x + 2)$$

$$x^3 - 4x^2 + x$$

$$(-) (+) (-)$$

$$\hline 2x^2 - 8x + 2$$

$$2x^2 - 8x + 2$$

$$(0)$$

$$x^4 - x^3 - 6x^2 - 17x + 5$$

$$x^4 - 4x^3 + x^2$$

$$(-) (+) (-)$$

$$\hline 3x^3 - 7x^2 - 17x + 5$$

$$3x^3 - 12x^2 + 3x$$

$$(-) (+) (-)$$

$$\hline 5x^2 - 20x + 5$$

$$5x^2 - 20x + 5$$

$$(0)$$

$$x^2 - 4x + 1 \mid x^2 + 3x + 5$$

32. (A,B,C) Given $p(x) = x^{2024} - y^{2024}$

$$p(y) = (y)^{2024} - y^{2024}$$

$$= y^{2024} - y^{2024}$$

$$p(y) = 0 \text{ (} x - y \text{) is a factor of } p(x)$$

$$p(-y) = (-y)^{2024} - y^{2024}$$

$$= y^{2024} - y^{2024}$$

$$p(-y) = 0 \text{ (} x + y \text{) is a factor of } p(x)$$

$$(x + y) \text{ and } (x - y) \text{ are factors of } p(x)$$

$$(x^2 - y^2) \text{ is also a factor of } p(x)$$

33. (A,B) Given $p(x) = x^3 q^2 - x^3 pt + 4x^2 pt - 4x^2 q^2 + 3xq^2 - 3x pt$

$$\therefore p(1) = q^2 - pt + 4pt - 4q^2 + 3q^2 - 3pt = 0$$

$$(x-1) \text{ is a factor of } p(x)$$

$$p(3) = 27q^2 - 27pt + 36pt - 36q^2 + 9q^2 - 9pt$$

$$= 0$$

$$\therefore (x-3) \text{ is a factor of } p(x)$$

34. (A,B,C)

Except option (D) all the lines don't pass through origin.

35. (A,C,D)

Square and rhombus are also parallelograms

REASONING

36. (C) Difference between the digits of 37 is $7 - 3 = 4$. In the others, this rule is not satisfied.

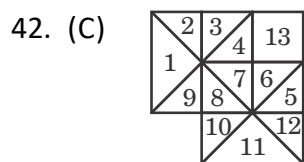
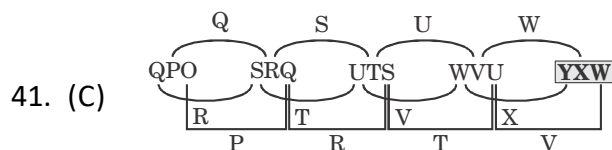
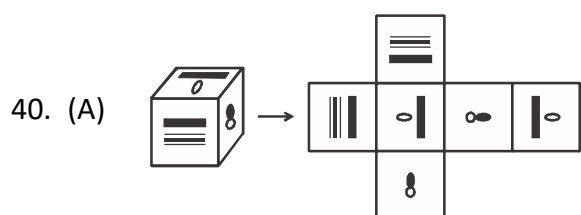
37. (D) $7^2 - 5^2 = 24$ | $22^2 - 20^2 = 84$
 $5^2 - 3^2 = 16$ | $11^2 - 9^2 = 40$

$6^2 - 4^2 = 20$ | $9^2 - 7^2 = 32$
 $3^2 - 1^2 = 8$ | $10^2 - 8^2 = 36$

38. (C) GEYAAWT – GETAWAY means 'a quick departure'.

E8t4e9C

39. (D) 
E8t4e9C



Small triangles \rightarrow ⑫

$2 + 3, 4 + 7, 7 + 6, 5 + 12, 10 + 8, 9 + 8$
 \rightarrow ⑥

$1 + 2 + 3, 8 + 10 + 11, 5 + 11 + 12, 1 + 8 + 9$
 \rightarrow ④

$2 + 3 + 4 + 7, 4 + 7 + 8 + 9, 6 + 7 + 8 + 10,$
 $7 + 6 + 5 + 12 \rightarrow$ ④

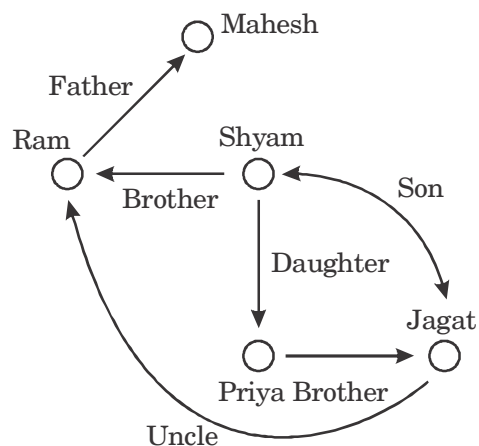
$2 + 3 + 4 + 7 + 13 + 6 + 5 + 12 \rightarrow$ ①

\therefore Total number of triangles

$= 12 + 6 + 4 + 4 + 1 = 27$


Hence, there are 27 triangles.

43. (C) Jagat is the brother of Priya and Priya is the daughter of Shyam. Therefore Shyam is the father of Jagat. Ram is the brother of Shyam. Therefore, Ram is the uncle of Jagat.



44. (B) Shapes in the right diagonal interchange and the two shapes in the left top corner and right bottom corner interchange places and top corner gets a new shape.

45. (D) Code for white fill is G, and code for hexagon is R.

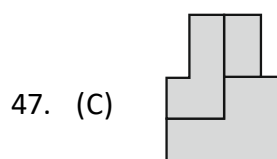
Hence, the code for  is **RG**.

CRITICAL THINKING

46. (B) Assertion (A): True. Large-scale stubble burning in neighboring states like Punjab and Haryana contributes to high pollution levels in Delhi and NCR, particularly during October and November.

Reason (R): True. Burning of organic material releases pollutants, and stubble burning does contribute significantly to air pollution in Delhi. However, plume from stubble burning does not consistently account for 70% of total air pollutants. It fluctuates depending on weather and wind patterns, and other pollution sources like vehicles, industries, and dust also play a significant role.

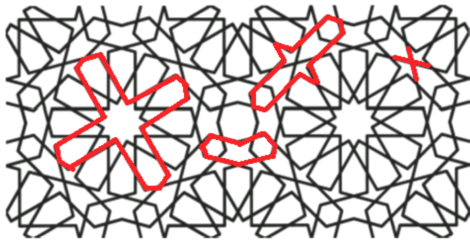
Since both (A) and (R) are true but (R) is not the correct explanation for (A), the correct answer is (B).



48. (D) As air escapes the available space is quickly replaced with water, so the tank's density becomes the same as that of the water and with the added weight and density of the tank itself continues to sink.



49. (B) (i), (iii), (v), (vi)



50. (A) Let's analyze each statement considering only one person is telling the truth.
1. If Aarav is telling the truth (Aarav didn't break the vase):
 - Aarav is telling the truth.
 - Bhavana is lying (Aarav didn't break the vase).
 - Charan is lying (Bhavana did break the vase).
 - Diya is lying (Charan is telling the truth).
 - This means Bhavana must have broken the vase, which contradicts Aarav's statement.
 2. If Bhavana is telling the truth (Aarav broke the vase):
 - Bhavana is telling the truth.
 - Aarav is lying (Aarav did break the vase).
 - Charan is lying (Bhavana did break the vase).
 - Diya is lying (Charan is telling the truth).
 - This means Aarav must have broken the vase, which doesn't lead to any

contradictions.

3. If Charan is telling the truth (Bhavana didn't break the vase):

- Charan is telling the truth.
- Aarav is lying (Aarav did break the vase).
- Bhavana is lying (Aarav didn't break the vase).
- Diya is lying (Charan is lying).
- This contradicts the assumption that only one person is telling the truth.

4. If Diana is telling the truth

(Charan is lying):

- Diya is telling the truth.
- Aarav is lying (Aarav did break the vase).
- Bhavana is lying (Aarav didn't break the vase).
- Charan is lying (Bhavana did break the vase).
- This means Bhavana must have broken the vase, which contradicts the assumption that Charan is lying about Bhavana.

Therefore, the only consistent scenario is when Bhavana is telling the truth, which means Aarav broke the vase.